

A' is the midpoint of BC
 B' is the midpoint of AC
 C' is the midpoint of AB

Then AA' , BB' and CC' are congruent at G (centroid)

Similarly for orthocentre, circumcentre, incentre

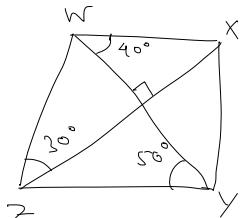
Angle Chasing :-

We have quadrilateral $WXYZ$ with $WY \perp XZ$.

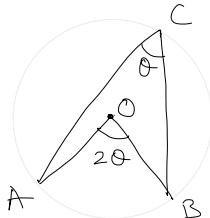
$$\angle WZX = 30^\circ, \angle XWY = 40^\circ, \\ \angle WYZ = 50^\circ$$

$$\text{Then, } \angle WZY = 180^\circ - 50^\circ - 90^\circ + 30^\circ = 70^\circ$$

$$\therefore \angle WXZ = 110^\circ \text{ (using cyclic quadrilateral)}$$



Theorem:- (Inscribed Angle Theorem)



$$\angle AOB = 2 \angle ACB$$

$$\text{Proof:- } \angle OAC = \angle OCA = \alpha \quad (\text{AO} = \text{BO} = \text{CO} = r)$$

$$\angle AOC = 180^\circ - \angle OAC - \angle OCA = 180^\circ - 2\alpha$$

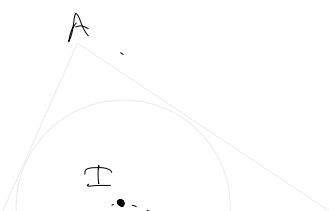
$$\text{Similarly, } \angle BOC = 180^\circ - 2\beta \quad (\angle OBC = \angle OCB = \beta)$$

$$\begin{aligned} \angle AOB &= 360^\circ - \angle AOC - \angle BOC \\ &= 360^\circ - (180^\circ + 2\alpha - 180^\circ + 2\beta) \\ &= 2(\alpha + \beta) \end{aligned}$$

$$\angle ACB = \angle OAC + \angle OCB = \alpha + \beta$$

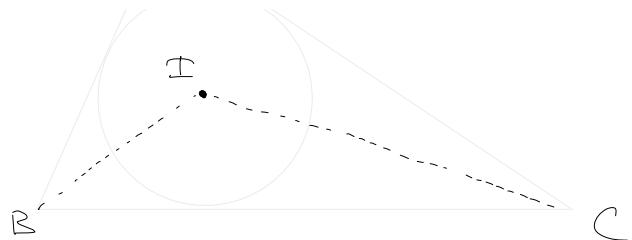
$$\Rightarrow \angle AOB = 2 \angle ACB$$

(Q) If I is the incentre of $\triangle ABC$, then that



Q) If I is the incentre of $\triangle ABC$ then show that

$$\angle BIC = 90^\circ + \frac{1}{2} \angle BAC$$



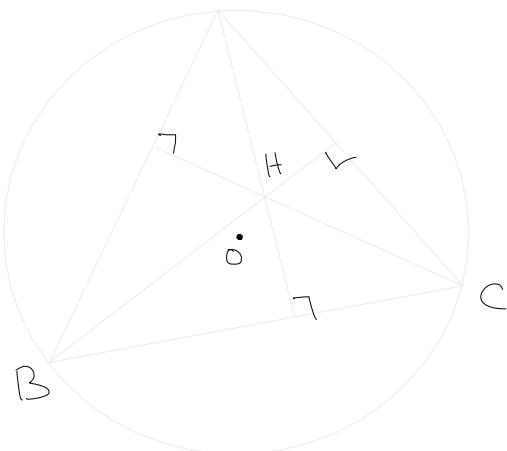
Ans:-

$$\begin{aligned}\angle BIC &= 180^\circ - (\angle IBC - \angle ICB) \\ &= 180^\circ - \frac{1}{2}(180^\circ - \angle BAC) \\ &= 90^\circ + \frac{1}{2} \angle BAC\end{aligned}$$

Q) Let $\triangle ABC$ be a triangle inscribed in a circle P. Show that $\overline{AC} \perp \overline{CB}$ iff \overline{AB} is a diameter of P.

Homework
Q) Let O and H denote the circumcentre and orthocentre of an acute $\triangle ABC$, respectively. Show that

$$\angle BAH = \angle CAO$$



O is circumcentre
i.e., centre of the circle.

Homework
Q) Let ABCD be a cyclic quadrilateral. A line L parallel to BC cuts AB and CD at E and F respectively. Show that ADFE are concyclic.